000 **Topo-Field:** Topometric mapping with Brain-inspired 001 **Hierarchical Layout-Object-Position Fields** 002

APPENDIX А

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SCENE PARTATION EXAMPLE A.1

The scene can be partitioned into different regions using walls as dividers and lines can be aligned to these walls. This is similar in most scenarios, making the annotation of scene regions a straightforward task as shown in Fig. A1.



Figure A1: Using walls as dividers to associate lines with them, the scene can be divided into various regions and 3D points can be labeled with related regions easily.

VISION-LANGUAGE EMBEDDINGS SIMILARITY OF REGION AND OBJECTS A.2

To demonstrate that the relationship of the vision-language and semantic embeddings for different regions is related to our intuition, we compare the similarity in region-region and object-region form and show the results in Fig. A2. It can be seen that based on general knowledge, cognitively related regions (e.g., the dining room and kitchen) and object-region pairs (e.g., sink and kitchen) are also more correlated in the vision-language and semantic feature spaces.

A.3 ABLATION STUDY

038 To explicitly encode the region information, we apply the LVM to process the background pixels out of the object bounding box and LLM to encode the region label text. What's more, for object 040 pixels, object label text is combined with the region text in the form of 'object in the region' before being encoded by LLM. To ablate the contribution of vision-language embeddings from CLIP 042 and semantic embeddings from Sentence-BERT in encoding region features, we compare different weight settings between the v-s embeddings when inferring the regions with 3D position inputs. Results are shown in Fig. A3. It can be seen that both vision-language embeddings and semantic 044 embeddings are indispensable, and weight settings with the greatest results are used for Topo-Field. 045

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A.4 HIERARCHICAL APPROACH COMPARISON

Hierarchical scene representation is widely studied with numerous tasks, mainly employing scalable receptive fields and representations to fine-tune results of scalable objects and local relations. As 051 Fig.A.8 shows, VoxFusion introduced octree map with various voxel sizes, LERF employed feature pyramids. As far as we know, few of them explicitly consider the layout level information and 052 the association with objects and positions. This idea comes from recent neuroscience findings, and similar theory has not yet been introduced in scene representations.



Figure A2: The similarity of a set of region embeddings (as shown in a) and object-region embeddings (as shown in b). The left graph shows the vision-language embedding similarity and the right one shows the semantic embedding similarity.

A.5 TOPOMETRIC SEARCH FOR PLANNING

We employ a simple A* approach for planning. Given a topometric graph G, the start point p, and the target destination object text t. First, the belonged region r of p is inferred according to the main paper. The existing objects nodes embeddings are compared with the encoded visual-language and semantic embeddings of t to find the target object node o. At the same time, if the region of destination object r_d is declared, the search process would be more simple by directly search among region nodes. Here lists the pseudocode of the employed A*.

A.6 TOPOMETRIC MAP NODES EXAMPLES

We list the attributes of nodes and edges in the topometric map as example here in Listing 1 - 4, including the object nodes, region nodes, and edges.

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112		
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114		
115		
116		
117		
118		
119		
120		-1 + C + c = 0
121	Alg	$\operatorname{gorithm} \mathbf{I} \operatorname{AStar}(G, r, o)$
122	1:	$openSet \leftarrow \{r\}$ \triangleright Set of nodes to be evaluated
123	2:	$cameFrom \leftarrow \{\}$ \triangleright Mapping of nodes to their parent nodes
124	3:	$gScore[r] \leftarrow 0$ \triangleright Cost from start along best known path
105	4:	$fScore[r] \leftarrow h(r, o)$ \triangleright Estimated total cost from start to goal
120	5:	while <i>openSet</i> is not empty do
126	6:	$current \leftarrow node in openSet$ with lowest $fScore$ value
127	7:	if $current = o$ then
128	8:	return ReconstructPath(cameFrom, o)
129	9:	end if
130	10:	remove <i>current</i> from <i>openSet</i>
131	11:	for each neighbor n of current do
132	12:	$tentativeGScore \leftarrow gScore[current] + d(current, n)$
133	13:	if $tentativeGScore < gScore[n]$ then
13/	14:	$cameFrom[n] \leftarrow current$
105	15:	$gScore[n] \leftarrow tentativeGScore$
135	16:	$fScore[n] \leftarrow gScore[n] + h(n, o)$
136	17:	if n not in openSet then
137	18:	add n to $openSet$
138	19:	end if
139	20:	end if
140	21:	end for
141	22:	end while
142	23:	return "No path found"
143	24:	function RECONSTRUCTPATH(cameFrom, current)
144	25:	$path \leftarrow [current]$
145	26:	while <i>current</i> is in <i>cameFrom</i> do
146	27:	$current \leftarrow cameFrom[current]$
1/7	28:	insert <i>current</i> at the beginning of <i>path</i>
1/0	29:	end while
140	30:	return <i>path</i>
149	31:	end function
150		
151		
152		
153		
154		
155		
156		
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158		
150		
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100		
161		



Figure A3: Ablation results on the accuracy of region prediction on Matterport3D? with 3D positions input. The w/o BG stands for not encoding background pixels to get region embeddings, and v-s weight ablates the weight of vision-language and semantic embeddings in the embeddings similarity contribution. Error bars show the results among samples from different scenes in Matterport3D?.

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```
216
           "id": 0,
     2
217
            "node_type": Entrance,
     3
218
            "bbox_extent": [
     4
219
                0.5,
     5
                1.6,
     6
220
                2.8,
     7
221
     8
            ],
222
            "bbox_center": [
     9
223
     10
                -3.244,
224
     11
                -0.276,
                0.487
225
     12
            ],
     13
226
            "class": "Entrance",
     14
227
           "caption": "Entrance connecting bedroom and living room."
     15
228
     16 },
229
                                      Listing 3: Entrance node
230
231
     1 {
232
            "id": 2,
     2
233
            "edge_type": region_entrance,
     3
            "start_node": {
234
     4
                "id": 0,
     5
235
                "node_type": region,
     6
236
                "bbox_extent": [
     7
237
                    4.163309999999999,
     8
238
                     4.207343,
     9
239
     10
                    2.53566175
                ],
     11
240
                "bbox_center": [
     12
241
                    -8.821845,
     13
242
                    2.6915385,
     14
243
                    1.259409125
    15
244
    16
                ],
                "region_tag": "bedroom"
    17
245
    18
            },
246
            "end_node": {
     19
247
                "id": 0,
    20
248
                "node_type": Entrance,
    21
                "bbox_extent": [
249
    22
                    0.5,
    23
250
     24
                    1.6,
251
                    2.8,
     25
252
     26
                ],
253
     27
                "bbox_center": [
254
     28
                    -3.244,
                    -0.276,
     29
255
                    0.487
     30
256
     31
                ],
257
                "class": "Entrance",
     32
258
                "caption": "Entrance connecting bedroom and living room."
     33
259
    34
            },
            "relationship": connected,
    35
260
     36
            "position_relation": "b to the southeast of a",
261
            "position_reason": "The x-coordinate of the center of bbox of
     37
262
           end_node (-3.244) is larger than that of start_node (-8.821845), and
263
           the y-coordinates of the center of bbox of end_node (-0.276) is less
           than that of start_node (4.207343). Therefore, b is to the southeast
264
           of a."
265
            "caption": "The pathway from bedroom to living room."
     38
266
     39 },
267
                                   Listing 4: Region entrance edge
268
269
     1 {
```

```
270
            "id": 2,
     2
271
            "node_type": object_region,
     3
272
            "start_node": {
     4
                "id": 7,
273
     5
                "node_type": object,
     6
274
                "bbox_extent": [
     7
275
                    2.155,
     8
276
                    2.052,
     9
277
     10
                     0.883
278
     11
                ],
                "bbox_center": [
     12
279
                    5.598,
     13
280
                     2.566,
     14
281
                     0.136
     15
282
     16
                1,
                "class": "bed",
283
    17
                "caption": "a bed with a white comforter and a pillow"
    18
284
            },
     19
285
     20
            "end_node": {
286
                "id": 0,
    21
287
                "node_type": region,
    22
                "bbox_extent": [
288
    23
                    4.163309999999999,
    24
289
                    4.207343,
     25
290
                    2.53566175
     26
291
                1,
     27
292
                "bbox_center": [
     28
293
     29
                    -8.821845,
                     2.6915385,
     30
294
                    1.259409125
     31
295
     32
                ],
296
                "class": "bedroom"
     33
297
                "caption": "A bedroom at the northwest of the house with warm
     34
           lighting. Main objects include a bed in the center, a large closet,
298
           and a dresser at the corner."
299
     35
            },
300
            "relationship": belong,
     36
301
            "position_relation": "a in the center of b",
     37
302
            "caption": "According to the bbox center position and extent, the bed
     38
303
            is in the center of bedroom."
     39 },
304
305
                                    Listing 5: Object region edge
306
307
       A.7 PROMPT EXAMPLE FOR REGION NODE CONNECTIVITY DESCRIPTION
308
309
       With topometric mapped nodes, we leverage LLM to describe the connectivity of nodes according
310
       to the general knowledge and bounding box 3D position. In listing 5, here we provide a prompt
311
       example to describe the connectivity relationship between content objects and regions and set up the
312
       edge.
313
     1 {
314
     2 DEFAULT_PROMPT_POST = """
315
     3 You are an excellent graph managing agent. Given a graph nodes set of an
316
           environment,
317
     4 you can explore the relationships of nodes with their attributes and
318
           build edges among
     5 them.
319
     6
320
     7 The input is a list of JSONS describing two types of nodes, including the
321
            object and
322
     8 region. You need to produce a JSON string (and nothing else) and set up
323
           edges between them with keys: "relationship", "position_relation" and
            "caption".
```

```
324
     9
325
    10 Each of the JSON fields will have the following fields:
326 11 1. id: a unique number
327
    12 2. node_type: type of this node
    13 3. bbox_extent: the 3D bounding box extents
328
    14 4. bbox_center: the 3D bounding box center
329
    15 5. class: an extremely brief description
330
    16 6. caption: a sentence describing node attributes in detail
331
    17
332
    18 Produce a "relationship" field that best describes the relationship of
          the object node and region node. Set "false" if the object is not
333
          related to the area or is not reasonable, the relationship is refused
334
          . Produce a
335
    19 "position_relation" field describing the position relationship between
336
          object and region according to their
    20 bounding box information in the 3D space. Before producing the "
337
          position_relation" field, produce a "caption" field that explains why
338
           the "position_relation" field is reasonable.
339
340
    22 The built edges should include following fields:
341 23 1. id: a unique number of each edge in order
342 24 2. node_type: according to the connected node type in the form "
          start_node\_end_node"
343
    25 3. start_node: keep JSON values of the object node unchanged
344
    26 4. end_node: keep JSON values of the region node unchanged
345
    27 5. relationship
346
    28 6. position_relation
347
    29 7. caption
    30 """
348
349
```

Listing 6: Prompt example to set up edge with nodes.

A.8 ADDITIONAL EXPERIMENT RESULTS

Additional experiments results of object localization using text query inputs and view localization using image query inputs. Also, a table is provided showing the metric on exactly each region class from 4 scenes in Matterport3D dataset.

Regions	Scene1			Scene2			Scene3			Scene4		
Regions	Acc.	Pre.	F1									
Living Room	0.948	0.970	0.959	0.870	0.881	0.875	0.778	0.810	0.793	0.902	0.949	0.925
Bedroom	0.943	0.825	0.880	0.925	0.923	0.924	0.687	0.767	0.725	0.920	0.870	0.894
Bathroom	0.466	0.680	0.554	0.903	0.898	0.901	0.875	0.463	0.605	0.797	0.831	0.814
Dining Room	-	-	-	0.961	0.794	0.870	0.774	0.732	0.752	0.933	0.887	0.910
Lobby	0.681	0.941	0.790	0.853	0.951	0.899	0.978	0.510	0.671	0.855	0.698	0.769
Family Room	-	-	-	-	-	-	0.903	0.571	0.700	0.926	0.936	0.931
Kitchen	0.994	0.654	0.789	0.788	0.836	0.811	0.833	0.833	0.833	0.758	0.854	0.803
Office	-	-	-	0.969	0.848	0.905	-	-	-	0.953	0.883	0.917
Toilet	-	-	-	-	-	-	0.900	0.711	0.795	-	-	-
vg. Acc./Samples	0.886 / 169k			0.900 / 185k			0.884 / 111k			0.894 / 112k		

Table 1: Region prediction results on the test set of different scenes from the Matterport3D? dataset. Accuracy, precision, and F1 score are used as metrics.





Figure A7: Text query localization on scene Apartment?.

VLMaps (Huang et al., 2023)

Topo-Field(Ours)

CLIP-Field (Shafiullah et al., 2022)

 Text query "Receptacle in the utility room

m

Text query "Heater in the bedroo

GT Region of Text



Figure A9: Image query localization on scene 2t7WUuJeko7?.



Figure A10: Image query localization on scene 17DRP5sb8fy?.



Figure A11: Image query localization on scene HxpKQynjfin?.